

Satellites that come to pass conformable to the calculus of *Cassini*, and differ days and hours from the calculus and predictions made upon the hypotheses of *Galilæi*: Besides that there should happen a great many which do not happen according to the system of *Cassini*. E.g. according to the hypothesis of *Galilæi*, the fourth of the Satellites should have more than 90 Eclipses in a year, of the duration of three or four hours; but according to the system of *Cassini*, the same Satellite will be three or four years without suffering any Eclipse. Which proceeds from nothing but the false situation of the Orbs supposed by *Galilæi*; as the great difference of the time of the Eclipses that happen depends from this, that neither *Galilæo* nor the other Astronomers do separate from the proper motion of the Satellites the appearances which do befall it by that of *Jupiter* about the Sun. And therefore 'tis, that they have taken for a simple and equal motion a motion compounded of an equal and unequal; whence they have slipped into an error about the Mean motions, which in progress of time hath so increased, that the Configurations drawn from their hypotheses for that time have almost no likeness at all with those that are observed.

These old hypotheses were therefore far off from serving to find the Longitudes, as their Authors intended them; since it was impossible for them nor only to observe the Eclipses of the Satellites for some years to the nearness of an hour, but even to make us know and distinguish at this time one Satellite from another, whereas by the System of Signor *Cassini* one may predict for many years to come the Eclipses of the Satellites with as much precision as those of the Sun and Moon by the Astronomical Tables.

*Methodus directa & Geometrica, cuius ope investigantur Aphelia, Eccentricitates, Proportionesque orbium Planetarum primiorum, absque supposita æqualitate anguli motus, ad alterum Ellipses focus, ab Astronomis hactenus usurpatæ. Auth. Edmundo Hally Jun. è Collegio Reginæ Oxon.*

**M**odus Terræ annus per Eclipticam, optima in æqualitatem inducit motibus cæterorum planetarum, Astronomis Copernicanis nomine Parallaxeos orbis notissimam; quam quidem inæqualitatem, ex observationibus non multâ operâ datam, methodi sequentis basin firmissimam constituo; ubi præter observata nihil aliud supponitur, quam quod orbes Planetarum sint Ellipses, quodque Sol in foco omnium orbibus communis, sit constitutus, & denique, quod tempora periodica singulorum

singulorum ita innescant, ut non sentiatur error aliquis, saltem in  
anibus vel tribus revolutionibus: His concessis, motus Terra, pro ceteris  
Planetis necessariò requisitus, primò aggregandus est.

TAB. I. Sit S Sol; ABCDE, orbis Terræ; P, Planeta Mars, (qui in hanc  
Fig. 2. rem plurimis de causis longè præferendus est;) & primò observetur  
verum tempus & locus, quo Mars opponitur Soli; tunc enim Sol &  
Terra coincidunt in lineam rectam cum Marte; vel, (quod fere semper  
accidit) si habuerit latitudinem, cum puncto, ubi perpendicularis à  
Marte demissa in planum Eclipticæ incidit. Sic in Schemate, S, A,  
& P sunt in linea recta; deinde post 68½ dies, Mars revertitur ad  
idem punctum P, ubi in priori observatione Soli opponebatur; Terra  
verò, cùm non revertatur ad A, nisi post 730½ dies, in B, Solem  
reßicit in linea SB, Martem verò in linea BP, & observatis longitudi-  
nibus Solis & Martis, omnes anguli Trianguli PBS dantur, & sup-  
posita PS 100000, in iisdem partibus invenitur longitudine linea SB;  
pari ratione post alteram Martis periodum, Terra existente in C in-  
venitur linea SC, nec absimiliter linea SD, SE, SF; differentiæque obser-  
vatorum locorum Solis, sunt anguli ad Solem ASB, BSC, CSD, DSE:  
Sic tandem ventum est ad hoc problema Geometricum: Datis tribus  
lineis, in uno Ellipseos foco coeuntribus, tam longitudine quam  
positione, invenire longitudinem transversæ diametri, cum distantia  
focorum: Cujus resolutio extenditur etiam ad reliquos planetas, si,  
post Theoriam motus Terræ cognitam, scrutemur (secundum methodum  
propositam à Reverendiss. Episcopo Sarisburensi in Astronomia ejus  
Geometricâ lib. 2. part. 2. cap. 5.) tres distantias planetæ alicuius à  
Sole in positionibus suis. Quoniam verò Rev. Episcopus supponit  
planetam ita fieri in orbe suo, ut equalibus temporibus æquales angulos  
ad focum alterum Ellipseos absolvet, & ei calculum suum superstruit,  
non incongruum videtur, ostendere, quomodo id ipsum fieri possit absque  
ista suppositione, quam observatio nos rejiciendam monet.

TAB. II. Fig. 3. Sit S, Sol; ALBK, orbis Terræ; P, Planeta, vel Punctum in plano  
Eclipticæ, ubi perpendicularis, à planeta demissa, incidit; AB linea  
Aphidum orbis Terræ: Observentur primò Planeta, in P, longitudine &  
latitude, simulque Solis Longitudo à Terra in K; & post periodum ejus-  
dem planetæ, Terra existente in L, observentur demum positiones Pla-  
netæ Solisque, ut prius: Nam ex observatis longitudinibus Solis &  
Aphelii Terræ, anguli ASK, ASL dantur, & consequenter latera SK, SL:  
(Nam si angulus Anomaliæ coequalis sit acutus, proportio est, ut differentia  
distantie medie & Co-sinus anguli in Eccentricitatem ducti, ad distan-  
tiam Aphelium, ita Perihelia distantia, ad distantiam Planetæ à Sole in  
data Anomalia: quæ si angulus fuerit obtusus, primus terminus propor-  
tionis

onis est summa duarum partium, quarum in priori analogia fuit differentia : Hujus Theorematis demonstrationem neminem Analytices modice peritum latere posse arbitror, & idcirco ei supersedeo:) Jam in Triangulo KSL dantur latera KS, LS, & angulus KSL, queruntur Latus KL, & anguli SKL, SLK: Deinde in Triangulo KLP, dantur KL, KLP, differentia observatarum Longitudinum planetæ, & PKL differentia angulorum SKL ultimo inventi, & SKP Elongationis Planetæ à Sole in prima observatione, queritur LP: Tum in Triangulo LSP, latera LS, LP, & angulus PLS elongatio Planetæ à Sole in secunda observatione, dantur; latus SP & angulus LSP requiruntur, quibus inventis, ut SP ad LP, ita Tangens Latitudinis observatae ex L, ad Tangentem Inclinationis sive Latitudinis ad Solem; & ut Co-sinus Inclinationis ad Radium, ita SP curtata distantia, ad veram distantiam planetæ à Sole: Sic tandem invenimus positionem & longitudinem desideratam. Jam restat ut ostendam, quomodo ex datis tribus distantiis à Sole cum angulis interceptis, invenienda sit media distantia cum Eccentricitate Ellipseos.

Sit S Sol, & SA, SB, SC tres distantie in debita positione, ductisque AB, BC, sit AB distantia focorum Hyperbolæ, & SA-SB=EH transversa diameter; quibus positis, describatur linea ista Hyperbolica, cuius focus interior est punctum A, extremitas lineæ longioris SA: Pari modo sint B, C, foci alterius Hyperbolæ, cuius diameter SB-SC=KL; ex quibus describatur linea Hyperbolica focum habens interiores in puncto B: Dico has duas Hyperbolas sic descriptas se se intersectare in puncto F, qui est alter Ellipseos quæ sita focus, ductaque linea FA, FB, vel FC, SA+FA, SB+FB vel SC+FC aequabitur transversæ diametro, & SF est distantia focorum: quibus positis descriptio Ellipseos facillima est. Cum verò hujus constructionis ratio non omnibus ita facile percipiatur, non abs re erit, illustrationem ejus aliquam afferre; Ideò dico, quid ex notissima Ellipseos proprietate SB+FE=SA+FA, & transpositis aequationis partibus FB-FA=SA-SB, ita ut etiamsi FB & FA nos lateant, earum tamen differentia aequalis sit SA-SB, hoc est, EH, cùmque sit ex natura Hyperbolæ, ut habeat quasvis duas lineas à suis focus ad quodvis punctum in sua curva constanter differentes quantitate transversæ diametri; constat, punctum F esse alicubi in curva Hyperbolæ, cuius diameter transversa aequatur SA-SB, & Foci A, B: Pari modo demonstrari potest punctum F esse in Hyperbola cuius diameter est SB-SC, & foci B, C. Ergo necesse est, ut sit in intersectione duarum istarum Hyperbolarum, que, cùm se se intersectent in unico solum punto, clare ostendunt ubi sit Focus alter Ellipseos quæ sita.

Jam ut id ipsum Analyticè expediatur, puta factum, si que FE=1, SA-SB=FB-FA=b, AB=c, SB-SC=FC-FB=d, BC=f, si que Sinus anguli ABC=S, Co-sinus ejusdem=s.

Tum

Tab.I.  
Fig.4.

Tum ut c ad b, ita  $2a-b$  ad  $\frac{2ab-bb}{c}$  &  $\frac{2a-bb+c}{2c} = BD$  per 36. 3 Eucl.  
& ut f ad d, ita  $2a+d$  ad  $\frac{2ad+dd}{c}$  &  $\frac{ff+2ad-dd}{2f} = BG$  per eandem, & ut mi-  
nuatur labor calculis sit  $\frac{cc-hb}{2c} = g$  &  $\frac{b}{c} = h$ , similiter sit  $\frac{ff-dd}{2f} = k$   
Per 12. &c. lib. 2. Eclid.  $\frac{d}{f} = l$ , tunc  $DE = g+ha$ , &  $BG = k-la$ ; & quoniam in omni

Triangulo Solutus angulo quadratum basis equatur summae  
acutus angulo summae differentia  
summae quadratorum laterum, & dupli rectanguli laterum in Co-  
sinum anguli comprehensi ducti, erit  $g+2gh+hha+kk-2kla+lla$   
 $+2gks-2glsat+khha-2hlsaa$  equalis quadrato DG: Sed DG aequalis  
est sinui Anguli DFG vel DBG in a, id est FB ducto, (est enim qua-  
drilaterum FBDG circulo, cuius diameter est FB, inscriptum;) ideo  
 $SSaa = gg + 2gh + hha + kk - 2kla + lla + 2gks - 2glsat + khha - 2hlsaa$ ;  
que aequatio facile resolvitur, cum non excedat quadraticam effectam,  
semperque componitur ex ipsis Quadratis & Rectangulis; signa tamen  
& ob diversam trium linearum constitutionem multa cautione  
sunt rectangulis adhibenda. Nostram aequationem aptavimus figu-  
ra IV, sed in alio quovis casu non erit difficile attendenti, ex iis  
que superius tradidimus, similem constituere. Sic tandem absoluvi  
propositum meum, & ostendi, quomodo ex tribus locis Heliocentricis  
Planetae, & distantias à Sole observatis, describi possit Orbita istius  
Planetae; quod non nisi quinque talibus observationibus hactenus effe-  
ctum vidi nus.

